

Cavity ring-down spectroscopy of H_2^{18}O in the range $16\,570\text{--}17\,120\text{ cm}^{-1}$ ☆

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Abstract

Cavity ring-down spectroscopy is used to record an absorption spectrum of H_2^{18}O water vapor in the $16\,570\text{--}17\,120\text{ cm}^{-1}$ region. In the spectrum, 596 lines are identified as belonging to H_2^{18}O , of which 375 lines are assigned by comparing to newly calculated theoretical lines. The spectrum covers the entire 5ν polyad and two new vibrational band origins, (321) at $16\,775.381\text{ cm}^{-1}$ and (401) at $16\,854.991\text{ cm}^{-1}$ are determined.

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1. Introduction

The absorption spectrum of water vapor is being comprehensively studied nowadays due to the high demand for accurate data for many aspects of science. Taking atmospheric science as an example, water vapor is the most important greenhouse gas and the major absorber of incoming sunlight. Besides the most abundant H_2^{16}O , its second most abundant isotopomer H_2^{18}O also contributes significantly to the absorption of solar radiation. Knowing the precise line positions and strengths of water isotopomers would therefore increase the accuracy of atmospheric modeling of the Earth as a whole. Furthermore, the 5ν region studied here lies in a window used for remote sensing [1]. H_2^{18}O has been much less extensively studied compared to H_2^{16}O and there has been no previous work on this isotopomer in this region.

The first experiment on H_2^{18}O at visible wavelengths was carried out in the early 1980s using the McMath Fourier transform spectrometer by Chevillard and co-workers at the National Solar Observatory (Kitt Peak,

AZ). They recorded long-pathlength spectra with isotopically enriched H_2^{18}O and H_2^{17}O samples over a wide frequency range and a series of papers have analyzed these experimental results [2–12]. The data on H_2^{18}O in the HITRAN2000 database [13] are limited, with the highest frequency listed for H_2^{18}O being $13\,900\text{ cm}^{-1}$ whereas for H_2^{16}O , the data extends to over $22\,600\text{ cm}^{-1}$. In addition, we found that this database appears to lack the entire 2ν polyad region of H_2^{18}O which Toth has extensively analyzed [6].

A recent analysis of the H_2^{18}O spectrum by Tanaka et al. [11] extended the frequency range analyzed up to $14\,520\text{ cm}^{-1}$, completely covering the $3\nu + \delta$ and 4ν polyads regions. In this study, pulsed cavity ring-down spectroscopy was used to record $16\,570\text{--}17\,120\text{ cm}^{-1}$ frequency range which covers the 5ν polyad region. Naus et al. [14] studied the same frequency region for natural abundance water. This work concentrated on H_2^{16}O lines but also tentatively identified some transitions due to H_2^{18}O .

2. Experimental details

The experimental apparatus used in this experiment is the same as the one used in the earlier measurements on H_2^{16}O [14]. Wavelength tunable laser pulses with a bandwidth of $\sim 0.06\text{ cm}^{-1}$, produced by a Nd:YAG

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pumped dye laser system (Quanta Ray PDL-3) were used in a generic pulsed CRD experiment. The ring-down cell was 86.5 cm long and a single mirror set, with reflectivities varying between 99.97% near $16\,500\text{ cm}^{-1}$ and 99.995% near $17\,000\text{ cm}^{-1}$, was used over the entire wavelength range. The radius of curvature of the mirrors is 1 m, and the stable cavity was aligned such that the statistics on the weighted residuals of a least squares fit were fully explained by contributions from Gaussian noise caused by the electronics and Poisson noise caused by the photon shot noise [15].

Before starting the measurements, the cell was heated to about $60\text{ }^{\circ}\text{C}$ and flushed with dry nitrogen to remove as much of the natural water vapor from the cell as possible, without risk of damage to the mirrors. The liquid isotope enriched water—Euriso-top 96.5% atom ^{18}O , 0.6% atom ^{17}O , 2.9% atom ^{16}O —was injected into the cavity while flushing the opening with a continuous dry nitrogen flow. The cell was then closed and partly evacuated, and several hours were allowed for the pressure to stabilize. In order not to lose isotopically enriched water, part of the dry nitrogen was left in the cell. The temperature in the cell was measured and the partial water vapor density in the cell was calculated assuming saturation density. The partial water vapor pressure at the set temperature corresponds to 24 mbar. To avoid condensation on the mirrors, the mirror mounts were gently heated.

Data points were taken at a step size of 0.008 cm^{-1} with averaging of five laser pulses at each laser frequency. The decay transients were detected using a photomultiplier tube, fed into a digital storage oscilloscope, and then transferred to a computer where a least squares fitting routine was used to estimate the decay rates. This fitting routine is the same as the one used in aligning the cavity. These decay rates contain both the water vapor absorption spectrum and a background signal caused by the losses of the empty cavity; this smooth background was subtracted from the spectrum before analyzing the resonance features. By recording an iodine spectrum simultaneously with the cavity ring-down spectrum a frequency calibration was obtained by comparing and interpolating the iodine spectrum against a reference atlas [16].

The spectra were searched by a computer program for possible locations of resonance features. A Voigt profile was then fitted to each of these candidate locations, yielding the central frequency, line width, and intensity. The entire spectrum was visually inspected to ensure that all fitted features were actual lines. Given the step size, the laser bandwidth and the width of the fitted lines, the one standard deviation error on the central frequency is estimated to be 0.01 cm^{-1} . The integrated line intensities, before correction associated with H_2^{16}O contamination in the sample, were calculated using the fitted line parameters. Several error contributions can be

distinguished in cavity ring-down spectroscopy: statistical effects, on the order of a few % in this experiment, a systematic underestimated absorption cross-section on narrow band absorbers [17] and saturation effects related to non-exponential decay in the ring-down transients of the strongest lines. An additional error that is specific for this experiment is the uncertainty in the isotopic content of the ring-down cell. An estimate of the isotope ratio of H_2^{16}O and H_2^{18}O is given below, but a few % uncertainty must be added to the error budget. The total error on the line intensities is estimated to be 15%. The complete list of lines containing both the center frequencies and loss-rates is available in the electric archive.

Despite our best effort to avoid contamination of the isotope enriched sample, several lines of H_2^{16}O were visible in the measured spectrum. To weed out these H_2^{16}O lines and identify which lines are H_2^{18}O lines, we compared our new spectrum with the previously measured spectrum, by plotting both in a single graph and manually assign each line to either H_2^{16}O or H_2^{18}O ; see Fig. 1 for a short portion of both spectra. In Fig. 1, the vertical axes are given in terms of a cross-section per molecule. From the integrated intensity ratio of the H_2^{16}O lines in both spectra, the isotope ratio in the spectra can be estimated. Using this approach yields a H_2^{16}O contamination of about 10%. The integrated line intensities in the full spectrum are corrected for the isotope ratio in the cell.

The comparison between the measurements on the two isotopes clearly shows that the H_2^{18}O lines are broader than the H_2^{16}O lines, the difference being caused by the pressure conditions during the measurements. The width of the lines is $\sim 0.13\text{ cm}^{-1}$ after fitting the spectra to a Voigt profile. This broadening beyond the laser linewidth of 0.06 cm^{-1} is a result of collision broadening. Doppler broadening and self-broadening at 24 mbar of water vapor yields a width of 0.09 cm^{-1} , the remainder of the broadening is attributed to nitrogen left behind in the cell during partial evacuation. The integrated intensities should be unaffected by the collisional broadening, and as the cell was saturated with water vapor, the density of the water vapor is known.

3. Line assignments

To help making line assignments, a new linelist for H_2^{18}O was generated using the DVR3D program suite [18]. The program requires an external potential energy surface (PES) and a dipole moment surface (DMS) and uses variational techniques to calculate rotation–vibration energy levels of triatomic molecules. A good PES is essential for accurate prediction of energy levels. In this study, we have used the PES developed by Shirin et al. [19]. This PES was fitted to an extensive dataset of

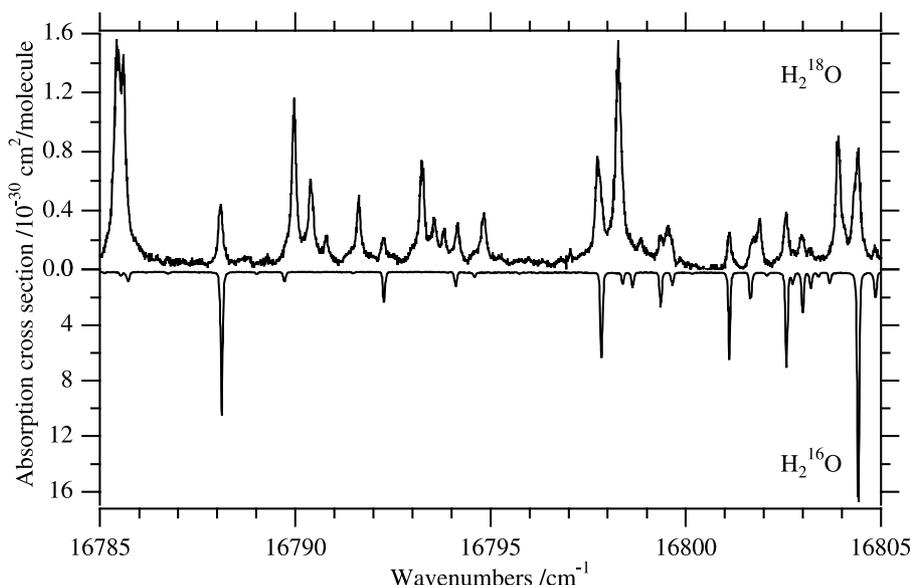


Fig. 1. A portion of the measured spectrum in H_2^{18}O enriched water (top), compared with the natural water vapor spectrum previously measured by Naus et al. [14] (bottom). Lines only present in the top graph are H_2^{18}O lines. The pressure at which the top graph was measured was 24 mbar, while the bottom graph was measured at about 16 mbar. The vertical axis in the top graph is a cross-section per molecule H_2^{18}O , the lines of H_2^{16}O in this graph are scaled with the isotope ratio.

H_2^{16}O energy levels including those generated from Naus et al.'s [14] cavity ring-down spectrum.

The following parameters were used to calculate the linelist. For vibrational states, Radau coordinates were selected. Thirty-four radial points based on a Morse oscillator-like functions [18] and 40 Gauss (associated) Legendre angular grid points were used to generate 2000 dimension final vibrational Hamiltonians. For rotationally excited states, the lowest 1000 vibrational functions were read for each value of k ($\approx K_a$) and final Hamiltonians of dimension $450 \times (J + 1)$ were diago-

nalized up to $J = 10$. A temperature of 296 K (room temperature) was used for calculations of transitions. Fig. 2 compares the measured H_2^{18}O absorption spectrum with our calculated linelist.

Initial assignments were made by comparing the experimental lines with the linelist, taking both frequency and intensity into consideration. Upper energy levels were then determined and all possible combinations of transitions were generated to search for further assignments by combination differences. Upper energy levels that were not confirmed by combination differences were

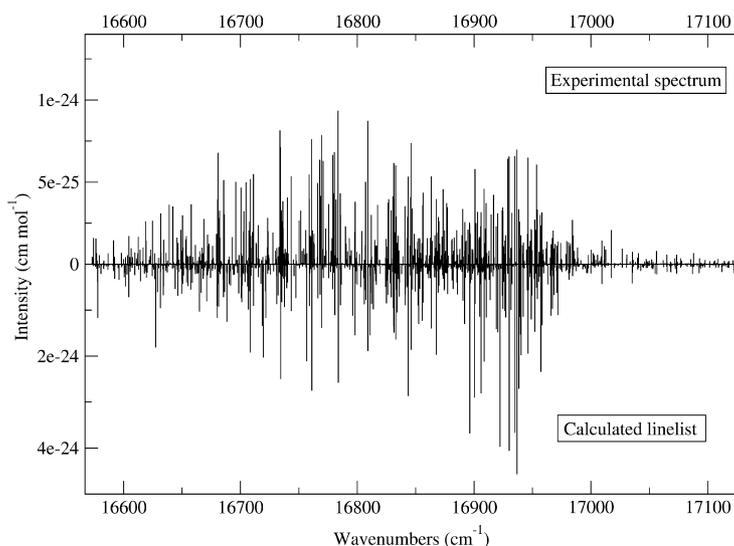


Fig. 2. Overview of the H_2^{18}O experimental spectrum and the calculated linelist in the $5v$ polyad region.

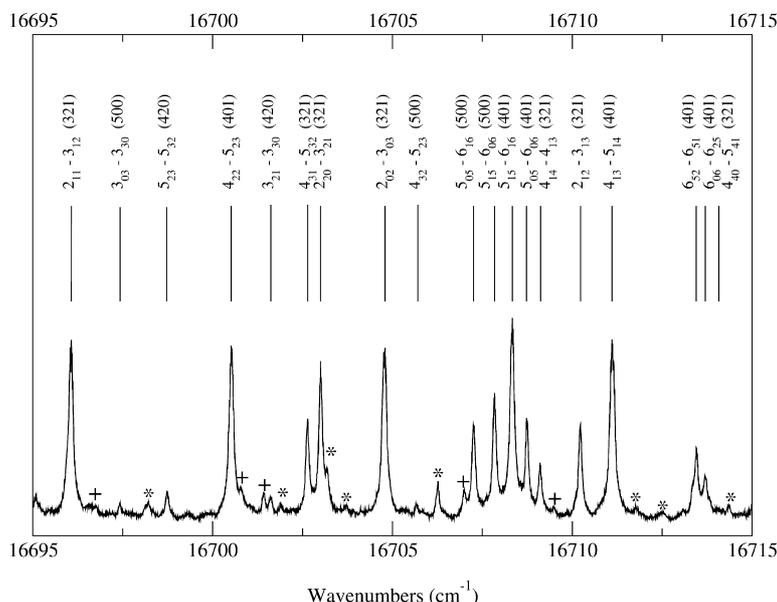


Fig. 3. Experimental spectrum in the 16 695–16 715 cm^{-1} range with the assignments. * indicates H_2^{16}O lines and + indicates unassigned H_2^{18}O lines.

re-considered and any necessary changes were made. Fig. 3 shows a part of spectrum with the assignments. The ratios of new energy levels of H_2^{18}O to known H_2^{16}O levels proved to be extremely helpful for checking the reliability of assignments, as it is known these ratios are approximately constant within a vibrational band [11].

We assigned 375 of the 596 H_2^{18}O lines to 10 different upper vibrational levels. Table 1 shows the summary of the result. All transitions originate in the (000) ground vibrational level. Two new vibrational band origins were determined directly by transitions to their 0_{00} states: (321) at 16775.381 cm^{-1} and (401) at 16854.991 cm^{-1} . The band origin for (500) can be estimated at $16854.84 \pm 0.02\text{ cm}^{-1}$ using the systematic error in our

Table 1
Summary of H_2^{18}O energy levels determined in this study

Band	Origin (cm^{-1})	No. of levels	No. of trans.
(340) or 30^+4	—	11	20
(241) or 30^-4	—	7	12
(043) or 21^-4	—	3	3
(142) or 21^+4	—	12	19
(222) or 31^+2	—	9	7
(420) or 40^+2	—	29	39
(321) or 40^-2	16775.381	42	83
(302) or 41^+0	—	1	2
(500) or 50^+0	16854.84	43	80
(401) or 50^-0	16854.991	50	110
Total		207	375

Bands are labeled using normal mode (left) and local mode (right) notations. No. of levels shows the number of newly determined energy levels. No. of trans. shows the number of transitions to the vibrational bands.

calculations. This procedure has been shown to work well in the past [20]. Table 2 shows the newly determined energy levels labeled with both normal and local mode notations. Obs – Calc shows the differences between an experimentally determined and the theoretically predicted energy level. All the assigned transitions and the energy levels can be found in the electronic archive.

4. Discussion and conclusion

The reliability of the new linelist was first tested by analyzing the H_2^{18}O spectrum in the $12\,400\text{--}14\,520\text{ cm}^{-1}$ range. In our previous study 747 of 927 lines were assigned using the linelist generated by Partridge and Schwenke [11]. With our new linelist, it was possible to make assignments to almost 900 lines. This test was particularly useful for checking the labeling of energy levels. Details will be given elsewhere [21].

Naus et al. assigned six of their transitions recorded using natural abundance water to H_2^{18}O . We find one of their lines was previously mis-assigned. The 16761.672 cm^{-1} line was assigned to $3_{13}\text{--}4_{14}\text{ 401--000}$ (H_2^{18}O) but the correct assignment is $5_{24}\text{--}5_{33}\text{ 142--000}$ (H_2^{16}O). The $3_{13}\text{--}4_{14}\text{ 401--000}$ (H_2^{18}O) line lies at 16761.004 cm^{-1} .

The absorption spectrum of H_2^{18}O recorded using the cavity ring-down spectroscopy has been analyzed. Five hundred and ninety-six lines were identified as H_2^{18}O and 375 of which are now assigned using the newly calculated linelist. The frequency range analyzed in this paper is the highest for H_2^{18}O to date and the results should be useful for atmospheric and other studies.

Table 2
 H_2^{18}O energy levels in cm^{-1} for the (321), (500), and (401) vibrational states

J	K_a	K_c	(321) or 40 ⁻ 2	Obs – Calc	(500) or 50 ⁺ 0	Obs – Calc	(401) or 50 ⁻ 0	Obs – Calc	
0	0	0	16775.381	1	0.431		16854.991	1	-0.259
1	0	1	16797.751	2	0.436	16876.838	16877.127	2	-0.165
1	1	1	16812.558	1	0.176	16887.674	16887.956	1	-0.180
1	1	0	16818.257	1	0.132	16892.781	16893.063	2	-0.173
2	0	2	16841.104	2	0.451	16919.565	16919.869	1	-0.202
2	1	2	16851.770	2	0.410	16926.727	16926.995	3	-0.166
2	1	1	16868.947	2	0.405	16941.961	16942.284	3	-0.164
2	2	1	16912.252	1	-0.042	16975.261	16975.532	1	-0.165
2	2	0	16913.804	2	0.281	16977.073	16976.948	3	-0.155
3	0	3	16903.088	2	0.423	16979.733	16980.198	2	-0.117
3	1	3	16905.182	2	0.061	16984.457	16984.835	2	-0.120
3	1	2	16943.465	2	0.392	17014.705	17015.001	2	-0.140
3	2	2	16979.495	3	0.285	17041.940	17041.964	2	-0.162
3	2	1	16986.445	2	0.249	17048.278	17048.333	1	-0.171
3	3	1	17115.166	2	-0.054	17059.953	17061.423	4	0.071
3	3	0	17115.365	2	-0.085	17060.270	17061.659	1	0.060
4	0	4	16979.033	2	0.384	17058.157	17058.363	1	-0.147
4	1	4	16983.912	1	-0.020	17060.221	17060.411	2	-0.163
4	1	3	17040.529	3	0.359	17109.231	17109.490	3	-0.159
4	2	3	17067.391	1	0.284	17129.480	17129.345	2	-0.145
4	2	2	17084.209	3	0.275	17145.664	17145.670	4	-0.131
4	3	2	17206.628	1	-0.292	17150.823	17151.466	3	-0.026
4	3	1	17208.361	3	-0.065	17152.405	17152.249	3	-0.057
4	4	1				17250.003	17250.636	1	-0.259
4	4	0	17318.857	2	0.217	17250.447	17250.811	1	-0.060
5	0	5	17076.303	1	0.033	17152.600	17153.584	3	-0.148
5	1	5	17077.137	1	0.403	17152.692	17153.671	3	-0.150
5	1	4	17157.904	3	0.310	17223.347	17223.609	3	-0.146
5	2	4	17175.241	3	0.252	17237.120	17236.784	4	-0.122
5	2	3	17207.731	4	0.259	17268.684	17268.425	2	-0.110
5	3	3	17321.491	4	0.146	17263.668	17264.399	4	-0.077
5	3	2	17326.788	2	-0.012	17269.334	17268.533	2	-0.401
5	4	2	17435.397	1	0.287	17363.369	17363.554	2	-0.343
5	4	1	17435.068	2	-0.256	17363.475	17363.609	2	0.065
5	5	1	17496.634	1	-0.217	17456.692	17456.947	2	-0.004
5	5	0				17456.703	17456.722	1	-0.236
6	0	6					17264.145	2	-0.133
6	1	6				17263.546	17264.166	2	-0.131
6	1	5	17293.138	3	0.238	17355.452	17355.477	3	-0.102
6	2	5				17364.686	17363.699	2	0.200
6	2	4					17411.992	3	-0.122
6	3	4	17458.118	3	-0.012	17399.119	17399.527	5	-0.077
6	3	3	17471.645	3	-0.019	17411.699	17409.519	1	-0.152
6	4	3				17499.669	17499.726	2	-0.341
6	4	2	17575.652	1	-0.385		17501.234	2	-0.374
6	5	2					17593.567	2	0.047
6	5	1					17593.561	2	-0.023
6	6	0					17726.192	1	-0.215
7	1	7					17391.441	2	-0.141
7	1	6				17503.917		2	0.237
7	2	6	17447.102	1	0.159				
7	3	5	17616.343	2	0.097				
7	3	4	17642.801	2		17575.265		3	-0.377
8	0	8					17535.562	2	-0.128

Also given are the number of transitions assigned to each level and the differences Obs – Calc, experimentally determined levels compared to our theoretical predictions.

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