

High Resolution Fourier Transform Spectrum of HDO in the 7500–8200 cm^{-1} region: Revisited

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Abstract

The HDO absorption FT spectrum is recorded and analyzed in the 7500–8200 cm^{-1} spectral region. The high accuracy *ab initio* calculation of Schwenke and Partridge was successfully applied for spectrum assignment that resulted in derivation of 508 precise rovibrational energy levels for the (300), (031), (111), (060), (220) and (002) states, with 295 of them being reported for the first time. In particular, eight new energy levels, including the band center at 7914.3170 cm^{-1} , were derived for the highly excited bending (060) state from transitions borrowing their intensities through local high-order resonance coupling with the (300) and (031) states.

Key words: vibration-rotation spectra, HDO molecule, water absorption

1 Introduction

Extensive calculations of the water vapor and its isotope species line positions and intensities performed by Schwenke and Partridge (SP)[1,2] initiated numerous theoretical and experimental investigations of the water vapor absorption spectra in different spectral regions. These calculations are very attractive for applications due to their high accuracy in terms of line position and intensity. At the same time the effective Hamiltonian (EH) approach traditionally used for the high-resolution spectra modeling often meets difficulties when applied to the highly excited interacting vibrational states of nonrigid molecules like water. The main problems in the EH method come from the divergence of

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the perturbation series in the presentation of the rotational Hamiltonian, as well as strong and numerous inter-polyad resonance interactions leading to a necessity to use much more effective parameters. The lack of the experimental information for the highly vibrationally excited interacting states of the HDO molecule also represents a serious obstacle in the EH approach.

The above mentioned reasons prevented complete identification and modeling of the high resolution spectrum of HDO. For example, many weak lines were left unassigned in the Fourier transform spectrum recorded and analyzed in the $7600 - 8100 \text{ cm}^{-1}$ spectral region in Ref. [3]. Meanwhile, the prediction power of the SP calculation is proved to be greatly helpful in the line-by-line analysis for HDO spectra in many regions[4–9]. In this paper, we present new theoretical and experimental study of the HDO Fourier transform absorption spectrum in the region $7500 - 8200 \text{ cm}^{-1}$. This time in the identification process we rely mainly on the SP calculation, which seems to be also very accurate in the considered spectral region.

As will be seen from the forthcoming sections, application of the detailed and accurate theoretical linelist to more extensive and accurate experimental data recorded at a higher resolution and better signal-to-noise ratio, resulted in retrieval of large set of new experimental energy levels for the (300), (031), and (111) vibrational states of HDO compared to Ref. [3].

2 Experimental Details

The sample of D_2^{16}O was purchased from PeKing Chemical Industry, Ltd. (China). The stated purity of deuterium was 99.8 %. The sample of HDO was prepared by mixing the D_2O and H_2O with a ratio of 1:1. The spectra were recorded at room temperature (296K) with the Bruker IFS 120HR Fourier-transform interferometer (Hefei, China), which is equipped with a path length adjustable multi-pass gas cell, a tungsten source, a CaF_2 beam-splitter, and Ge diode detector. The unapodized resolution was 0.01 cm^{-1} , and the apodization function was Boxcar. The sample pressure was 10hpa which was measured by a manometer with a stated accuracy of 20 Pa. The total path length was 87m. To improve the signal-noise-ratio, 2040 scans were accumulated.

Since in the region under study there are many absorption lines due to the H_2O and D_2O , the spectrum of “pure” D_2O was also recorded to identify the absorption lines of HDO. The spectrum was calibrated with H_2O lines in this region listed in the Hitran database. The precision in the positions of unblended lines was estimated better than $1 \times 10^{-3} \text{ cm}^{-1}$. For illustration, a small piece of the recorded spectra is presented on Fig.1.

3 Spectrum Assignment and Energy Levels Derivation

For identification purpose approximate intensities were derived for each observed line from the peak absorption values. Synthetic HDO spectrum from Ref.[1,2] was used as the input data for the expert system for automatic assignment of the rovibrational molecular spectra.

Since a large number of the observed energy levels were derived from a single line without ground state combination differences(GSCD), it is worth to give some details of the identification process here. Obviously, the reliable identification of single lines entirely depends on the accuracy of the simulated spectrum used in the assignment process. To the best of our knowledge, the SP prediction of the line positions and intensities of water vapor and its isotope species is one of the most accurate among recent *ab initio* and variational calculations, at least for wavenumbers lower than 16000 cm^{-1} . Although the accuracy of the SP calculation of line positions varies significantly depending on the spectral region and the isotope species considered (see, for example, [10]), these variations behave regularly with the V_1, V_2, V_3 vibrational, and the J, K_a rotational quantum numbers. This gives the opportunity to introduce the correcting factor for SP prediction for each vibrational band.

Another important point in the weak line identification process is the matching between the observed and calculated intensities. In case of intensity consideration, one should estimate an intensity threshold — I_1 in calculated data that means that all calculated lines with $I \geq I_1$ should be observed in the spectrum or their absence can be explained by the overlapping with stronger lines in their vicinity. Another threshold — I_2 can be introduced for the weakest lines, so all calculated lines with intensity $I_2 \leq I < I_1$ either can be found or be absent in the spectrum, and all calculated lines with intensity $I < I_2$ can be neglected. Obviously, that I_2 should be close to the noise level of the spectrum. On the other hand, we should not find in the observed spectrum those lines, which can not be explained within the estimated accuracy of the synthetic spectrum. If these rules hold for simulated spectrum, one can rely on this calculation without running the risk of making wrong assignment.

The synthetic spectrum for considered spectral region was found to be of the high quality. In Table 1 an average and maximum deviation between the observed and calculated positions is presented for all considered vibrational states of HDO in this region. As shown in Table 1, the averaged deviations for most of the analyzed states do not exceed 0.07 cm^{-1} , that is quite satisfactory for the unambiguous line identification since we found that the observed and calculated values of line intensities also match well. In our case the I_2 and I_1 values were estimated to be of $5.0\text{E-}07$ and $4.0\text{E-}06\text{ cm}^{-2}\text{ atm}^{-1}$ respectively. Comparison of the observed and calculated spectrum in the whole region is

shown on Fig. 2.

Finally 1254 absorption lines of HDO were rotationally assigned and they correspond to 1415 transitions going on 5 upper vibrational states (see Table 1). The resulting linelist, which includes observed HDO line positions and calculated [2] intensities followed by rovibrational assignment, is attached to this paper as Supplemented Material. The HDO lines blended by the D₂O lines are specially marked. Some relatively strong HDO lines were not included into the linelist since they are unrecoverably blended by stronger lines of other isotope species.

Extensive set of 508 precise experimental energy levels of HDO was derived by adding the ground state experimental energy levels [11] to the observed transitions. This number should be compared with 135 energy levels obtained in Ref. [3] (see Table 1). The observed energy level values are presented in Tables 2-3 together with the experimental uncertainties and number of lines used for level determination. As a comparison, the experimental uncertainty indicated by the GSCD method is about $4 \times 10^{-4} \text{ cm}^{-1}$ on average, which is significantly better than in our previous contribution [3]. For the (002) state earlier investigated in Ref. [12] only 22 new (compared to Ref. [12]) energy levels are shown of 102 observed.

As it was stressed in Ref. [3], the strong interaction between (031) and (111) vibrational states results in greatly mixed wave-functions and ambiguity in vibrational assignment of their rotational levels. We accepted here the rovibrational assignments proposed by SP, which may differ in some cases from those given in Ref. [3]. An interesting example of the high-order local rovibrational resonance represents the (300)-(060) interaction. This coupling affects the $K_a = 0$ energy levels of both states and induces reasonable intensity transfer to the otherwise extremely weak transitions of the $6\nu_2$ band. As J and K_a increase, the (031)-(060) coupling also becomes important. In addition to Ref. [3] data we could derive eight energy levels of the highly excited (060) state (see Table 3) with $K_a=0,1$ and 2 including the band center at $7914.3170 \text{ cm}^{-1}$.

At the final stage of the spectrum analysis we could partly assign transitions of the very weak (220)-(000) band. Eighteen energy levels were derived for the (220) vibrational state, which seemed to be strongly perturbed by resonance coupling with other states. In particular, the high K_a energy levels of the (300) state (not observed in Ref. [3]) are strongly coupled to the corresponding levels of the (220). The (002) energy levels have the largest average and maximum deviations from the SP prediction (see Table 1). However, these deviations vary very slowly and regularly with J and K_a that allowed us to perform reliable assignments which were also confirmed by the EH calculations [13].

4 Conclusion

Usage of the high accuracy Schwenke and Partridge [1,2] calculation for the theoretical treatment of the Fourier transform absorption spectrum of HDO molecule in the 7500–8200 cm^{-1} spectral region provided complete assignment of the experimental data and derivation of the extensive set of new precise energy levels for the (300), (031), (111) states. Some additional energy levels were also obtained for the highly excited (060) and (220) states. This new HDO energy level set represents enlargement of the existing data and can be used in further refinement of the water vapor potential function, while detailed HDO absorption linelist in the 7500–8200 cm^{-1} spectral region supplements the information contained in the spectroscopic databases like HITRAN compilation.

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Fig. 1. Part of the spectrum of HDO. Upper panel: observed spectrum; Lower panel: stick spectrum from *ab initio* calculation by Schwenke and Partridge[1,2]. Transitions of HDO are assigned while D₂O lines are indicated with “D”. Note that some strong lines are beyond the display range.

Fig. 2. Overview of the HDO spectrum between 7500 and 8200 cm⁻¹. (a) Stick spectrum retrieved from the FTS spectrum recorded with a 87 m absorption path length at a total pressure of water of 10 hPa (D:H≈1:1). (b) Stick spectrum from *ab initio* calculation by Schwenke and Partridge[1,2].

Table 1

Deviations between the observed and calculated (SP, Ref. [1,2]) energy levels for the HDO vibrational states in the considered region.

V ₁	V ₂	V ₃	Band center, cm ⁻¹		Number of Observed Levels		$E_{obs} - E_{calc}$, cm ⁻¹	
			E_{obs}	E_{calc}	This work	Ref.[3]	Average	Maximum
0	0	2	7250.5192	7250.640	102		0.14	-0.22
0	3	1	7754.6055	7754.630	111	11	0.00	±0.03
1	1	1	7808.7586	7808.730	103	37	0.01	+0.04
0	6	0	7914.3170	7914.365	10	2	0.03	-0.06
3	0	0	7918.1719	7918.135	164	83	0.06	-0.18
2	2	0		8090.034	18		0.07	+0.10

Table 2
 Rotational energy levels (in cm⁻¹) of the (300), (031), and (111) vibrational states of HDO

$J K_a K_c$	E_{obs} cm ⁻¹ (300)	$\sigma \times 10^3$ cm ⁻¹	N	E_{obs} cm ⁻¹ (031)	$\sigma \times 10^3$ cm ⁻¹	N	E_{obs} cm ⁻¹ (111)	$\sigma \times 10^3$ cm ⁻¹	N
0 0 0	7918.1719		1	7754.6055		1	7808.7586		1
1 0 1	7932.8872	0.1	2	7770.0448	0.6	2	7824.1053	2.6	2
1 1 1	7946.6145	0.7	2	7789.2029	0.2	2	7840.9318	0.1	2
1 1 0	7949.0716	0.1	2	7792.4604	0.3	2	7843.9931	0.4	2
2 0 2	7962.2634	0.3	3	7800.5240	0.2	3	7854.4164	0.2	2
2 1 2	7973.4633	0.6	3	7816.7599	0.1	3	7868.5855	0.2	3
2 1 1	7980.8263	0.3	4	7826.5117	0.6	2	7877.7446	0.1	2
2 2 1	8022.6185	0.2	2	7929.4767	0.1	2	7880.7671	0.1	4
2 2 0	8022.9129	0.2	4	7929.8454	0.1	2	7881.1278	0.5	3
3 0 3	8004.2474	0.1	3	7845.2879	1.2	3	7898.9523	0.8	2
3 1 3	8013.5499	0.1	4	7857.8590	0.1	2	7909.8405	0.1	3
3 1 2	8028.2391	0.1	4	7877.2686	1.1	2	7928.3441	0.2	3
3 2 2	8066.5185	0.1	5	7975.7249	0.1	3	7926.5378	0.2	4
3 2 1	8067.9604	0.4	5	7977.5292	0.4	2	7928.5832	0.4	6
3 3 1	8142.0179	0.1	2	8073.9264	2.5	2	8017.0379	0.1	3
3 3 0	8142.0393	0.2	2	8074.0623	1.1	3	8017.0678	0.3	2
4 0 4	8060.2222	0.2	3	7903.3697	0.3	3	7956.8161	0.2	3
4 1 4	8066.6864	0.3	3	7912.2573	0.1	2	7964.4609	0.3	2
4 1 3	8091.0188	0.1	3	7944.3139	0.1	2	7994.9607	0.1	2
4 2 3	8124.7992	0.2	4	8037.0823	0.1	3	7987.5453	0.4	3
4 2 2	8128.9428	0.3	9	8042.2400	0.1	2	7993.0072	0.2	2
4 3 2	8200.9727	0.1	4	8136.5558	0.4	2	8078.5373	0.3	3
4 3 1	8201.1254	0.1	3	8136.4740	0.1	2	8078.7557	0.3	3
4 4 1	8305.1165	0.2	2	8275.8404	0.2	3	8194.5927	0.4	3
4 4 0	8305.1156	0.7	2	8275.8384	0.3	2	8194.5919	0.6	2
5 0 5	8128.5183	0.1	3	7973.9086	0.9	3	8027.2378	0.1	2
5 1 5	8132.6631	0.2	3	7979.6895	0.3	2	8032.1865	0.1	2
5 1 4	8168.7285	0.1	3	8027.0248	0.1	2	8077.4149	0.2	2
5 2 4	8197.2465	0.2	3	8113.2939	0.3	2	8063.1567	0.4	4
5 2 3	8206.2607	0.1	6	8124.3820	0.1	3	8074.8498	0.6	4
5 3 3	8274.7739	0.2	6	8214.9765	0.4	2	8155.5026	1.6	2
5 3 2	8275.3689	0.4	5	8215.4116	0.2	2	8156.3555	0.6	2
5 4 2	8378.6132	0.4	3	8354.2027	1.0	3	8271.0682	1.1	2
5 4 1	8378.6254	0.1	3	8354.2614	0.2	2	8271.0753	0.7	3
5 5 1	8510.9579	0.4	2	8530.6453	0.2	2	8413.6540	0.6	2
5 5 0	8510.9563	0.2	2	8530.6468	1.2	2	8413.6530	0.3	2
6 0 6	8208.7655	0.2	4	8056.3869	0.1	2	8109.7735	0.3	3
6 1 6	8211.2727	0.1	4	8059.8977	0.1	2	8112.7750	0.1	2
6 1 5	8260.7653	0.3	3	8124.5504	0.6	3	8174.9171	0.1	2
6 2 5	8283.6025	0.2	3	8204.0516	0.4	3	8153.0928	0.1	2
6 2 4	8299.9813	0.2	4	8222.9915		1	8174.1073	1.6	4
6 3 4	8363.6432	0.1	3	8309.1418	0.2	3	8247.7629	0.6	3
6 3 3	8365.1502	0.1	4	8310.8843	0.2	2	8250.3224	1.0	4
6 4 3	8466.9589	0.2	4	8448.3924	0.3	3	8362.9616	0.1	2
6 4 2	8467.0205	0.4	2	8448.7355	0.2	2	8362.8178	0.2	2
6 5 2	8598.8148	0.1	2	8624.4269	1.1	2	8505.0336	0.2	2
6 5 1	8598.8142	0.7	2	8624.4263	1.7	2	8505.0341	0.7	2
6 6 1	8759.0094	0.1	3	8833.1236		1	8674.2375		1
6 6 0	8759.0094	0.1	3	8833.1236		1	8674.2375		1
7 0 7	8300.9173	0.1	5	8150.6417	0.2	2	8204.2820	0.2	2
7 1 7	8302.3484	0.3	3	8152.6679	0.5	2	8206.0152	0.1	2
7 1 6	8366.3833	0.4	5	8286.5722	1.3	2	8235.8491		1
7 2 6	8383.5814	0.1	4	8309.0149	0.1	2	8256.9764	0.2	2
7 2 5	8409.8214	0.1	4	8342.9073		1	8290.3012	2.5	2
7 3 5	8466.5714	0.1	2	8418.9312		1	8355.8086	0.1	4
7 3 4	8471.1290	0.4	5	8423.4728	0.6	2	8361.2035	0.5	2

$J K_a K_c$	E_{obs} cm ⁻¹ (300)	$\sigma \times 10^3$ cm ⁻¹	N	E_{obs} cm ⁻¹ (031)	$\sigma \times 10^3$ cm ⁻¹	N	E_{obs} cm ⁻¹ (111)	$\sigma \times 10^3$ cm ⁻¹	N
7 4 4	8570.2377	0.1	3	8558.3956	0.1	2	8470.1379	0.2	2
7 4 3	8570.4518	0.2	4	8560.2253	2.4	3	8470.8922	0.2	3
7 5 3	8701.4024	0.8	2				8611.7671		1
7 5 2	8701.4052	0.7	2	8733.9465		1	8611.7782	0.5	2
7 6 2	8861.0423	0.2	2	8942.2256	3.0	2	8780.3866	0.3	2
7 6 1	8861.0426	0.1	2	8942.2256	3.0	2	8780.3860	0.2	2
7 7 1	9047.9232	0.2	2				8975.4544	1.2	2
7 7 0	9047.9232	0.2	2				8975.4544	1.2	2
8 0 8	8404.9487	0.1	2	8256.7045	0.2	2	8310.7838	0.2	2
8 1 8	8405.7394	0.1	2	8257.8295		1	8311.7476	1.0	2
8 1 7	8484.6326	0.2	2	8411.4595	0.8	2	8359.8175	0.2	3
8 2 7	8496.8835	0.2	3	8427.8272	0.6	2	8374.4107	0.3	3
8 2 6	8535.2616	0.2	3	8476.6489		1	8422.4980	0.1	2
8 3 6	8584.4192	0.2	3	8544.1189	0.6	2	8479.1498	1.6	2
8 3 5	8592.5515	0.3	4	8553.7271	0.1	2	8489.6431	1.4	2
8 4 5	8688.7211	0.2	3	8683.9150	0.1	2	8593.8321	0.1	3
8 4 4	8689.2931	0.2	3	8683.9889	0.1	2	8594.5139	0.2	2
8 5 4	8818.7628	0.6	3	8859.1147		1	8733.9143		1
8 5 3	8818.7818	0.4	2	8859.1941		1	8733.9481		1
8 6 3	8977.7104	1.8	2	9066.9427		1	8901.7761	2.7	3
8 6 2	8977.7069	1.6	2	9066.9427		1	8901.7787	0.6	2
8 7 2	9163.9544		1				9096.2111		1
8 7 1	9163.9544		1				9096.2111		1
8 8 1	9376.6430		1						
8 8 0	9376.6430		1						
9 0 9	8520.9219	0.9	2	8374.6501		1	8429.3253	0.2	3
9 1 9	8521.3455	0.1	2	8375.2576	0.5	2	8429.8443	0.1	3
9 1 8	8615.0643	0.3	2	8548.8015	0.5	2	8495.5755		1
9 2 8	8623.1552	0.4	2	8560.1306	2.1	2	8505.0147	1.9	2
9 2 7	8675.6248	0.1	3	8627.7840	1.3	2	8571.4422	1.8	2
9 3 7	8716.5584	0.2	2	8684.3500	0.1	2	8615.4950		1
9 3 6	8731.2516	0.4	2	8701.9607	8.4	2	8635.6543	2.1	2
9 4 6	8820.5873	0.8	2				8732.4949	1.0	2
9 4 5	8822.0998	0.1	3				8734.4312		1
9 5 5	8950.9577	1.0	2	9000.0916		1	8871.5066		1
9 5 4	8951.0087		1				8871.6331		1
9 6 4	9109.0289	3.1	2	9207.2868		1			
9 6 3	9109.0343	1.8	2	9207.2873		1			
9 7 3	9294.5122	0.3	2						
9 7 2	9294.5119	0.5	2						
9 8 2	9506.4541		1						
9 8 1	9506.4541		1						
9 9 1	9744.0518		1						
9 9 0	9744.0518		1						
10 0 10	8648.8589	0.1	2	8504.5555		1	8559.9499	0.1	2
10 1 10	8649.0817	0.3	4	8504.8664		1	8560.2212	0.1	2
10 1 9	8757.1060	0.7	3	8698.1163	1.4	2	8642.7237		1
10 2 9	8762.1923	1.3	2	8705.6028	0.1	2			
10 2 8	8830.0581	0.9	2	8793.0070	0.6	2			
10 3 8	8862.6989	0.1	2	8839.8877		1	8767.1630		1
10 3 7	8887.4378	0.3	2	8867.9057	3.0	2	8799.0637		1
10 4 7	8968.7028	1.0	2				8885.7178		1
10 4 6	8972.1544	0.3	2	8987.4482		1	8891.0983	1.1	2
10 5 6	9097.9584	0.5	2						
10 5 5	9098.1687	0.5	2	9157.3095		1	9024.9251		1
10 6 5	9255.0239		1	9363.2540		1			
10 6 4	9255.0346		1	9363.2567		1			
10 7 4	9439.6070		1						
10 7 3	9439.6071		1						

$J K_a K_c$	E_{obs}	$\sigma \times 10^3$	N	E_{obs}	$\sigma \times 10^3$	N	E_{obs}	$\sigma \times 10^3$	N
	cm^{-1}	cm^{-1}		cm^{-1}	cm^{-1}		cm^{-1}	cm^{-1}	
	(300)			(031)			(111)		
11 0 11	8788.7708	0.1	2	8646.4372		1			
11 1 11	8788.8868	0.3	2	8646.6004		1	8702.8109	0.2	2
11 1 10	8910.6516	0.2	2	8859.1970		1			
11 2 10	8913.7058	0.4	2	8863.9556	1.8	2			
11 2 9	8997.8507	0.8	2	8973.9347		1			
11 3 9	9022.5648	0.1	2	9008.8965		1			
11 3 8	9059.1873	0.6	2	9049.9359		1			
11 4 8	9131.2681	0.2	2	9158.3159		1			
11 4 7	9138.1446	0.4	2						
11 5 7	9259.8456	0.8	2						
11 5 6	9260.3898		1						
11 6 6	9415.7669		1						
11 6 5	9415.7772		1						
11 7 5	9599.2361		1						
11 7 4	9599.2363		1						
12 0 12	8940.6520	0.4	2				8857.4994	0.1	2
12 1 12	8940.7067	1.6	2				8857.5771		1
12 1 11	9075.7355	0.3	3	9032.0095		1			
12 2 11	9077.4934		1	9034.9726		1			
12 2 10	9178.0456		1	9164.7969		1			
12 3 10	9196.3503		1	9191.3435		1			
12 3 9	9244.5555		1						
12 4 9	9308.2763		1						
12 4 8	9320.6861		1						
12 5 8	9436.6126		1						
12 5 7	9437.8584		1						
12 7 6	9773.4386		1						
12 7 5	9773.4396		1						
13 0 13	9104.4639		1				9024.3994		1
13 1 13	9104.5117		1				9024.4472		1
13 1 12	9252.4347	4.3	2	9216.6782		1			
13 2 12	9253.4422		1	9218.5109		1			
13 2 11	9367.1298		1						
13 3 11	9380.7672		1						
13 3 10	9447.6649		1						
13 4 10	9499.4768		1						
13 4 9	9519.9991		1						
13 5 9	9628.1676		1						
14 0 14	9280.2049		1						
14 1 14	9280.2253	3.6	2						
14 1 13	9440.8411	0.8	2						
14 2 13	9441.3939		1						
14 2 12	9571.6776		1						
14 3 11	9663.2365		1						
15 0 15	9467.8220	1.1	2						
15 1 15	9467.8293	3.2	2						
15 2 14	9641.3298		1						
16 0 16	9667.2765		1						
16 1 16	9667.2817		1						

N is the number of lines used for the upper energy level determination and σ denotes the corresponding experimental uncertainty in 10^{-3} cm^{-1} .

Table 3
Rotational energy levels (in cm-1) of the (060), (002), and (220) vibrational states of HDO

$J K_a K_c$	E_{obs} cm ⁻¹	$\sigma \times 10^3$ cm ⁻¹	N	$J K_a K_c$	E_{obs} cm ⁻¹	$\sigma \times 10^3$ cm ⁻¹	N	$J K_a K_c$	E_{obs} cm ⁻¹	$\sigma \times 10^3$ cm ⁻¹	N
	(060)			4 4 0	8558.7062		1	12 8 5	9277.2901		1
0 0 0	7914.3170		1	5 0 5	8305.5911		1	12 8 4	9277.2891		1
1 0 1	7929.8972		1	5 2 4	8404.7408		1	12 9 4	9485.5166		1
2 0 2	7960.5925	0.3	3	5 2 3	8415.1744		1	12 9 3	9485.5166		1
3 0 3	8007.4630	0.3	3	5 5 1	8800.9838		1	13 2 11	8750.3185		1
4 0 4	8067.8172	0.8	2	5 5 0	8800.9838		1	13 7 6	9290.6896		1
4 1 3	8141.4562		1	6 1 6	8392.7248		1	13 8 6	9475.2787		1
5 0 5	8142.0631		1	6 1 5	8455.8198		1	13 8 5	9475.2755		1
6 0 6	8230.5251	2.0	3	7 0 7	8480.4521		1	13 9 5	9682.4269		1
7 1 7	8347.0643		1	7 1 7	8484.1664		1	13 9 4	9682.4269		1
7 2 5	8556.1889	0.6	3	8 0 8	8585.4354		1	14 4 10	9139.4178		1
	(220)			9 0 9	8702.1795		1	14 5 9	9223.0272	0.5	2
2 2 0	8225.1342		1		(002)			15 3 12	9298.8667		1
3 0 3	8178.9222		1	10 8 3	8926.9617		1	15 4 11	9383.7530		1
3 2 2	8270.0021		1	10 8 2	8926.9644		1	15 5 11	9441.3283		1
4 0 4	8236.0140		1	11 8 4	9094.5143		1	15 5 10	9463.5777		1
4 2 2	8335.0522		1	11 8 3	9094.5141		1	15 6 10	9577.6308		1
4 4 1	8558.7081		1	12 5 7	8794.9786	0.3	2				

N is the number of lines used for the upper energy level determination and σ denotes the corresponding experimental uncertainty in 10^{-3} cm⁻¹. For the (002) state only 22 new (compared to Ref. [12]) energy levels are shown of 102 observed.